

ECE 111 - Homework #14

ECE 311 Filters

Filter Analysis

1) A filter has the following transfer function

$$Y = \left(\frac{500(s+1)}{(s+6)(s+7)(s+8)} \right) X$$

- 1a) What is the differential equation relating X and Y?
- 1b) Find y(t) assuming $x(t) = 4$
- 1c) Find y(t) assuming $x(t) = 4 \sin(5t)$

2) Plot the gain vs. frequency for this filter from 0 to 30 rad/sec.

$$Y = \left(\frac{500(s+1)}{(s+6)(s+7)(s+8)} \right) X$$

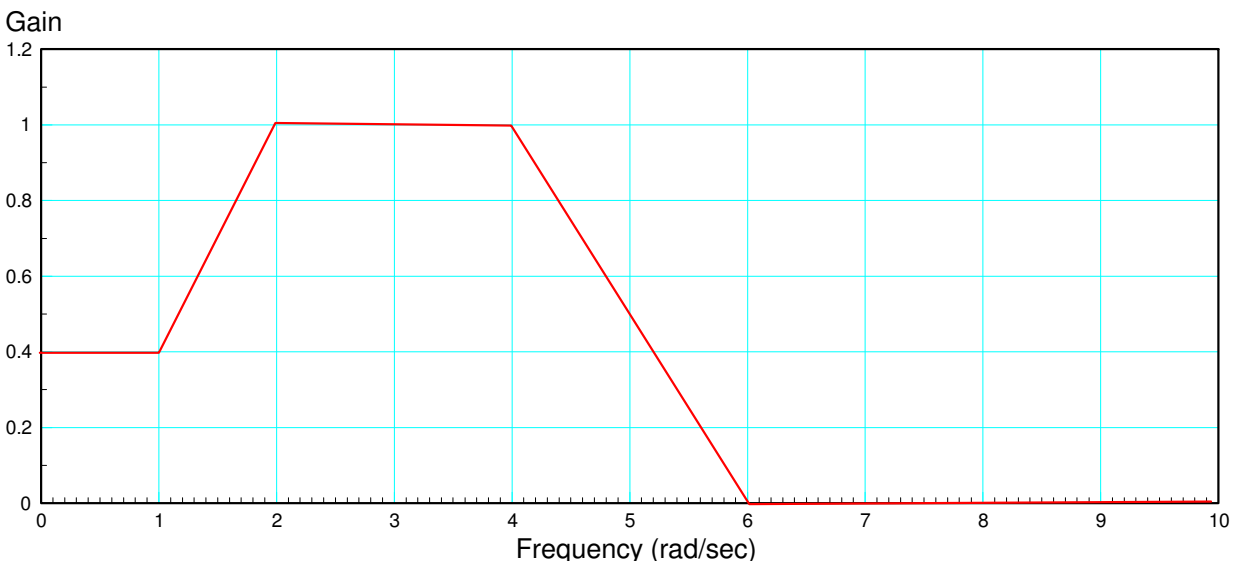
3) Plot the gain vs. frequency for this filter from 0 to 30 rad/sec.

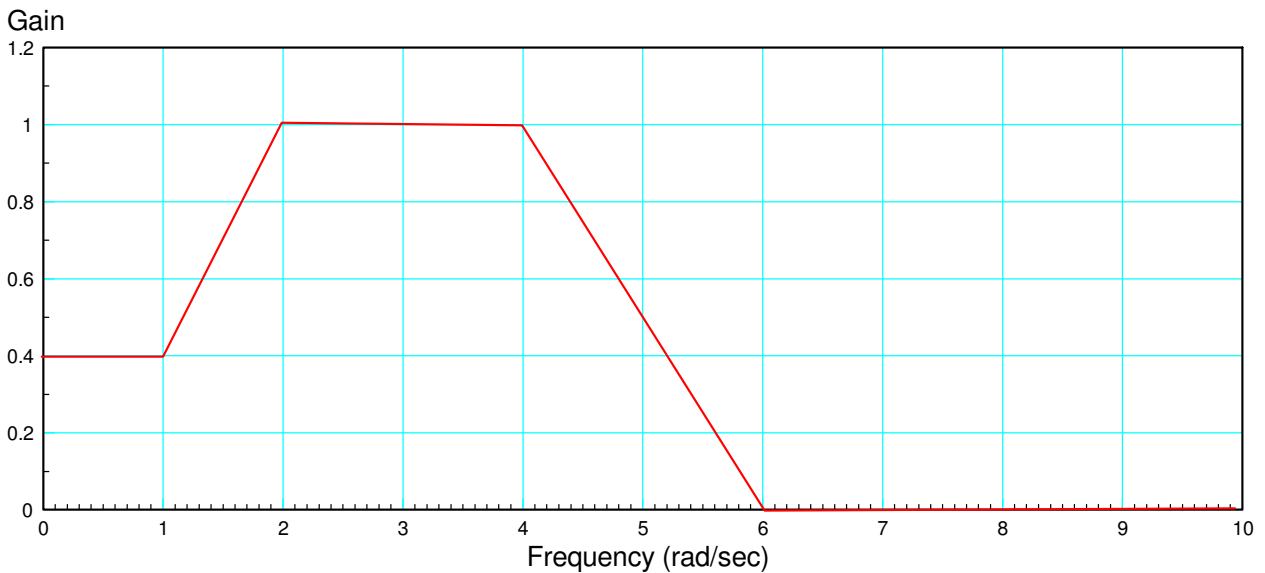
$$Y = \left(\frac{100(s^2+400)}{(s^2+2s+25)(s^2+4s+100)} \right) X$$

Filter Design

Problem 4-6) Design a filter of the following form so that the gain matches the graph below:

$$G(s) = \left(\frac{a}{(s^2+bs+c)(s^2+ds+e)(s^2+fs+g)} \right)$$





4) Write an m-file, `cost.m`, which

- Is passed an array, `z`, with each element representing (a, b, c, d, e, f, g)
- Computes the gain, $G(s)$ for this value of (a, b, c, d, e, f, g)
- Computes the difference between the gain, G , and the target (above), and
- Returns the sum-squared error in the gain

5) Use your m-file to determine how 'good' the following filter is:

$$G(s) = \left(\frac{a}{(s^2 + bs + c)(s^2 + ds + e)(s^2 + fs + g)} \right) = \left(\frac{1000}{(s^2 + 2s + 5)(s^2 + 2s + 17)(s^2 + 2s + 37)} \right)$$

6) Use `fminsearch()` to find the 'best' filter of the form

$$G(s) = \left(\frac{a}{(s^2 + bs + c)(s^2 + ds + e)(s^2 + fs + g)} \right)$$

- Give the resulting (a, b, c, d, e, f, g)
- Give the resulting filter, and
- Plot the 'optimal' filter's gain vs. frequency