

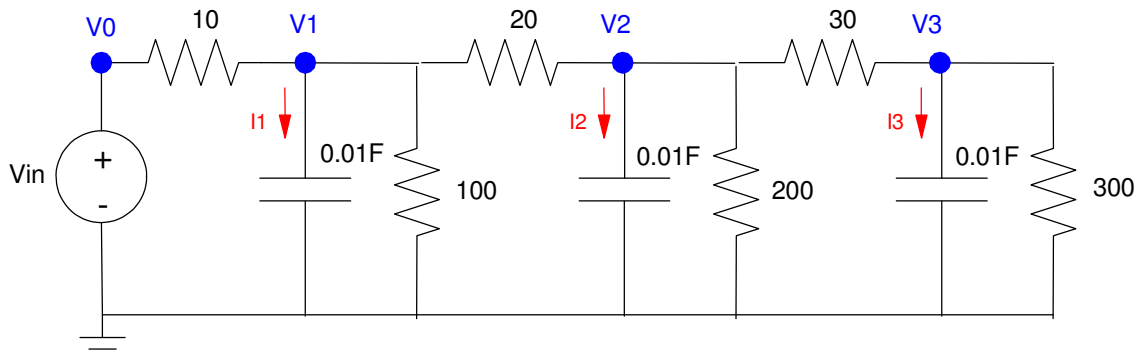
Homework #6: ECE 461/661

Electric Circuits, Mass-Spring Systems, Rotational Systems. Due Monday, September 29th

RC Circuits

1) Express the dynamics of the following circuit in state-space form

- Find the transfer function from V_{in} to V_3



Problem #1

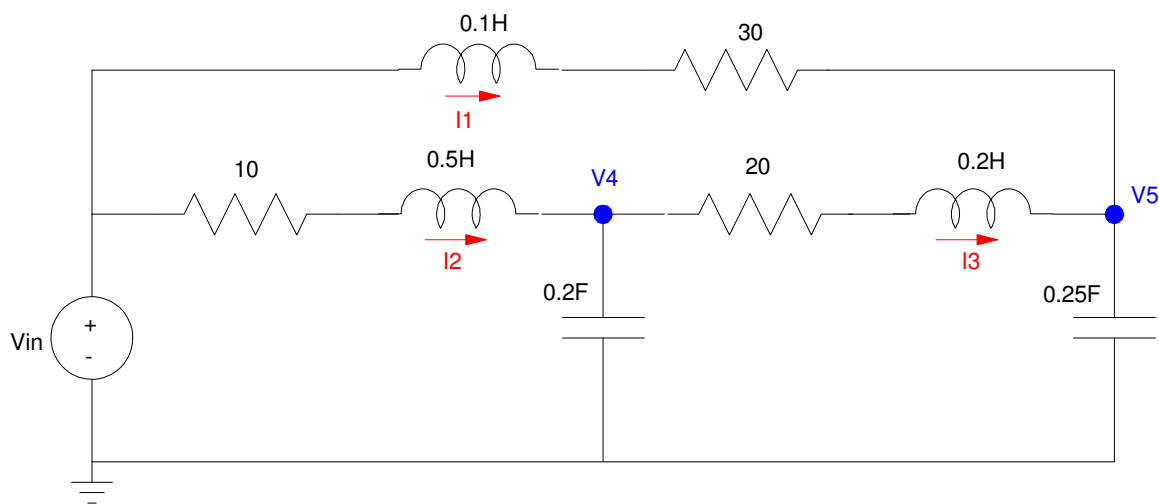
RLC Circuits

2) Express the dynamics of the following circuit in state-space form

- Find the transfer function from V_{in} to V_5

3) Assume $V_{in} = 0$. Specify the initial conditions so that the total energy at $t = 0$ is 1.0 Joules and

- The transients decay as slow as possible
- The transients decay as fast as possible

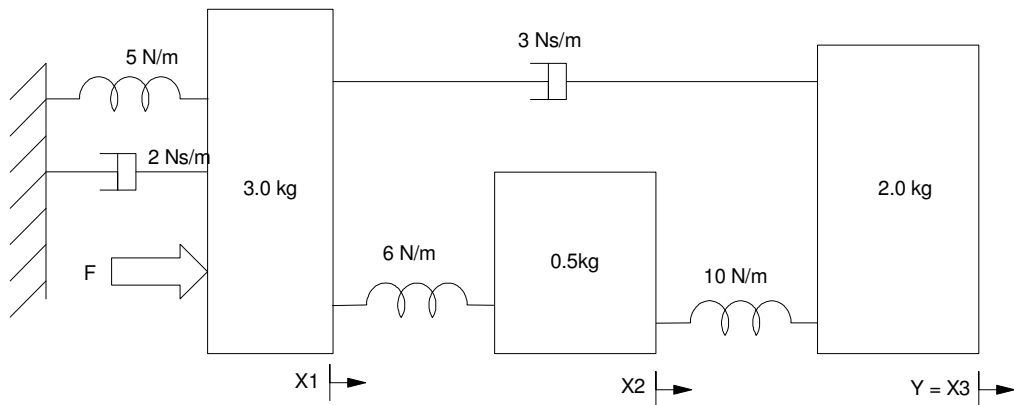


Problem #2 and #3

Mass Spring systems

4) Draw the circuit equivalent for the following mass-spring systems.

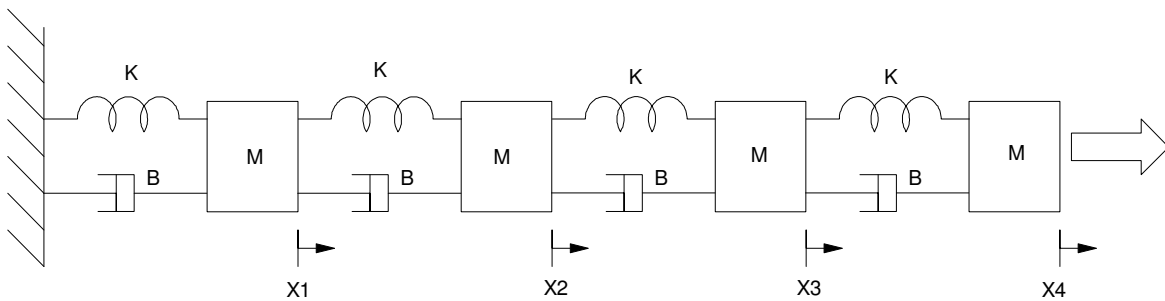
- Express the dynamics in state-space form
- Find the transfer function from F to X_2
- Plot the step response from F to X_2



Problem 4

5) Draw the circuit equivalent for the following mass-spring systems.

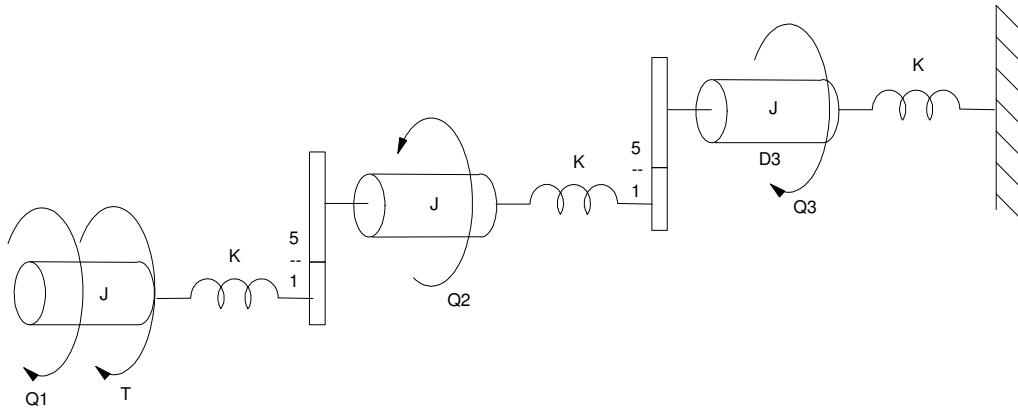
- Express the dynamics in state-space form
- Find the transfer function from F to X_4
- Plot the step response from F to X_4



Problem 5: $M = 2.0\text{kg}$, $B = 0.3\text{ Ns/m}$, $K = 10\text{ N/m}$

Rotational Systems

- 6) Draw the circuit equivalent for the following rotational system.
- Express the dynamics in state-space form
 - Find the transfer function from T to Q_1
 - Plot the step response from T to Q_1



Problem 6: $J = 2.5 \text{ Kg m}^2 / \text{s}^2$. $K = 20 \text{ Nm/rad}$, $D_3 = 1.5 \text{ Nms/rad}$

Motors - Skip problem 7 & 8 (homework set is long enough as it is)

~~7) Find the transfer function for the following DC servo motor~~

~~<http://www.baldor.com/catalog/CDP3306>~~

~~Allen Bradley CDP3306: 1/4 HP Servo Motor~~

- ~~\$716ea~~
- ~~$K_t = 1.117 \text{ ft-lb} @ 1.68\text{A}$~~
- ~~$R_a = 8.54 \text{ Ohms}$~~
- ~~$L_a = 60.59\text{mH}$~~
- ~~$J = 4.680 \text{ lb-ft}^2$~~
- ~~$1.43\text{A} @ 1690\text{rpm} @ 0.945 \text{ ft-lb load}$~~
- ~~$0.1\text{A} @ 180\text{V} @ 1830\text{rpm} @ 0 \text{ ft-lb load}$~~
- ~~Weight 23.0kg~~

~~8) Assume this motor is used to power an electric bicycle at 20mph~~

- ~~Motor speed @ 20mph = 1750 rpm~~
- ~~Gear (wheel) used to convert 1750 rpm to 20mph~~
- ~~Bicycle weight = 100kg~~

~~What is the gear reduction (wheel diameter) to convert 1750rpm to 20mph?~~

~~What is the inertia relative to the DC servo motor (bring the 100kg mass back to the motor through a gear)~~

~~What is the transfer function (dynamics) for the bicycle / servo motor combination?~~