

ECE 111 - Homework #15

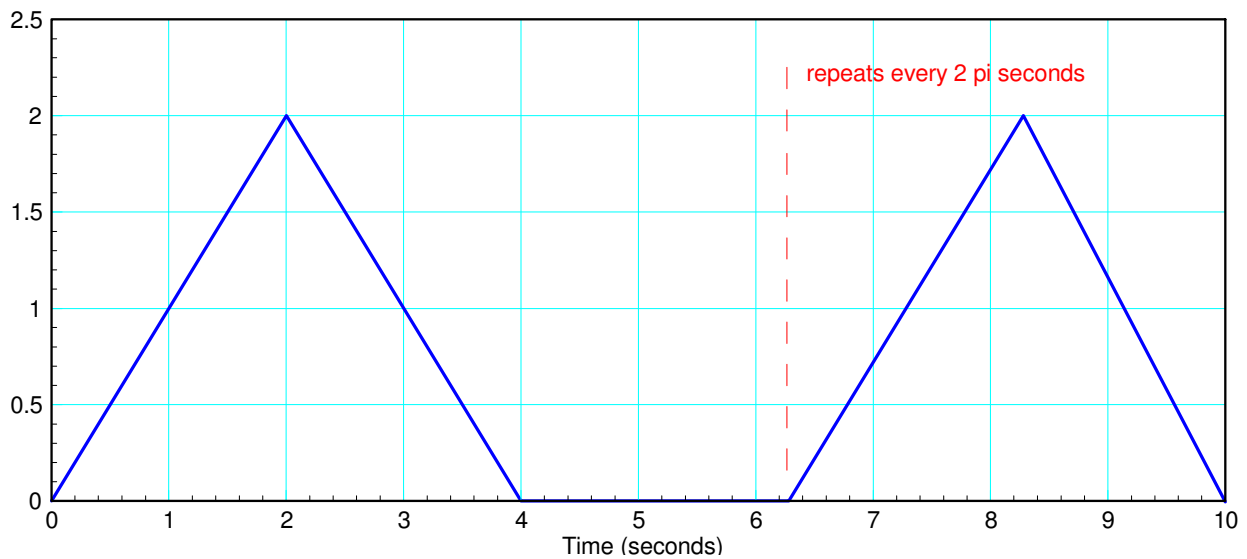
Week #11 - Signals & Frequency Content of a Signal
Due Monday, May 5th. Please submit via email or on BlackBoard

Problem 1-5) Let $x(t)$ be a function which is periodic in 2π as shown below

$$x(t) = x(t + 2\pi)$$

or in Matlab:

```
t = [0:0.001:2*pi]' + 1e-9;  
x = t .* (t<2) + (4-t) .* (t>2) .* (t<4);  
plot(t,x)
```



$x(t)$ Note that $x(t)$ repeats every 2π seconds

Curve Fitting with a power series:

1) Using least squares, approximate $x(t)$ over the interval $(0, 2\pi)$ as

$$x(t) \approx a_0 + a_1 t + a_2 t^2 + a_3 t^3 + a_4 t^4 + a_5 t^5$$

Plot $x(t)$ along with its approximation.

Curve Fitting using a Fourier Series

2) Using least squares, approximate $x(t)$ over the interval $(0, 2\pi)$ as

$$x(t) = a_0 + a_1 \cos(t) + b_1 \sin(t) + a_2 \cos(2t) + b_2 \sin(2t) + a_3 \cos(3t) + b_3 \sin(3t)$$

Plot $x(t)$ along with its approximation.

Superposition

3) Assume X and Y are related by

$$Y = \left(\frac{0.5}{s^2 + s + 0.5} \right) X$$

3a) Determine $x(t)$ in terms of its Fourier Transform out to 3 rad/sec

3b) Plot $x(t)$ and its Fourier approximation taken out to 3 rad/sec

4) Determine the output, $y(t)$, at DC ($\omega = 0$)

5) Determine the output, $y(t)$, at 1 rad/sec

6) Determine the output, $y(t)$, at 2 rad/sec

7) Determine the output, $y(t)$, at 3 rad/sec

8) Determine the total answer, $y(t)$

- Plot $x(t)$ and $y(t)$